



13th Confluence Competition

Raúl Gutiérrez

Aart Middeldorp

Naoki Nishida

Teppei Saito

René Thiemann

<https://project-coco.uibk.ac.at/2024>

Outline

- 1. Acknowledgements**
- 2. History**
- 3. 2024**
- 4. Awards**
- 5. Outlook**

Acknowledgements

- ▶ CoCo 2024 tool authors

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- ▶ Fabian Mitterwallner

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 - ▶ Geoff Sutcliffe
- ▶ Aaron Stump

Outline

1. Acknowledgements

2. History

3. 2024

4. Awards

5. Outlook

2012

TRS





CPF

<input type="checkbox"/> ACP	✓												
<input checked="" type="checkbox"/> CSI	✓	✓											
<input type="checkbox"/> Saigawa	✓												
<input checked="" type="checkbox"/> CeTA		✓											

2013

TRS

CPF

 ACP	✓												
 CSI	✓	✓											
 Saigawa	✓												
 CeTA		✓											

2014

TRS

CPF

CTRS

<input type="checkbox"/>	ACP	✓	✓										
<input checked="" type="checkbox"/>	CSI	✓	✓										
<input type="checkbox"/>	Saigawa	✓											
<input checked="" type="checkbox"/>	CeTA		✓										
<input type="checkbox"/>	CoLL	✓											
<input checked="" type="checkbox"/>	ConCon		✓	✓									
<input type="checkbox"/>	CO3			✓									

2015

TRS

CPF













CTRS












HRS











GCR
















NRS

	TRS	CPF	CTRS	HRS	GCR	NRS							
● ACP	✓	✓											
▬ CSI	✓	✓											
▬ CeTA		✓											
● CoLL-Saigawa	✓												
▬ ConCon		✓	✓										
⊖ CO3			✓										
▬ CoScart			✓										
● ACPH				✓									
▬ CSI ^{ho}				✓									
● AGCP					✓								
● NoCo						✓							

	TRS	CPF-TRS	CTRS	HRS	GCR	NRS	UN	CPF-CTRS				
 ACP	✓	✓										
 CSI	✓	✓					✓					
 CeTA		✓						✓				
 CoLL-Saigawa	✓											
 ConCon			✓					✓				
 CO3			✓									
 CoScart			✓									
 ACPH				✓								
 CSI ^{ho}				✓								
 AGCP					✓							
 Nrbox						✓						
 FORT					✓		✓					















	TRS	CPF-TRS	CTRS	HRS	GCR	NFP	UNR	CPF-CTRS	UNC			
 ACP	✓	✓										
 CSI	✓	✓				✓	✓		✓			
 CeTA		✓						✓				
 CoLL-Saigawa	✓											
 ConCon			✓					✓				
 CO3			✓									
 ACPH				✓								
 CSI ^{ho}				✓								
 AGCP					✓							
 FORT					✓	✓	✓		✓			
 SOL				✓								

	TRS	CPF-TRS	CTRS	HRS	GCR	NFP	UNR	CPF-CTRS	UNC			
 ACP	✓	✓	✓						✓			
 CSI	✓	✓				✓	✓		✓			
 CeTA		✓						✓				
 CoLL-Saigawa	✓											
 ConCon			✓					✓				
 CO3			✓									
 CSI^ho				✓								
 AGCP					✓							
 FORT					✓	✓	✓		✓			
 SOL				✓								

	TRS	CPF-TRS	CTRS	HRS	GCR	NFP	UNR	CPF-CTRS	UNC	COM	INF	SRS
 ACP	✓	✓	✓						✓	✓		✓
 CSI	✓	✓				✓	✓		✓			✓
 CoLL										✓		
 CeTA		✓						✓				
 CoLL-Saigawa	✓											✓
 ConCon			✓					✓			✓	
 CO3			✓								✓	
 infChecker											✓	
 maedmax											✓	
 CSI ^{ho}				✓								
 AGCP					✓							
 Moca											✓	
 FORT					✓	✓	✓		✓	✓		
 noko-leipzig												✓
 nonreach											✓	

2020

TRS CPF-TRS CTRS HRS GCR NFP UNR CPF-CTRS UNC COM INF SRS

	TRS	CPF-TRS	CTRS	HRS	GCR	NFP	UNR	CPF-CTRS	UNC	COM	INF	SRS
 ACP	✓	✓	✓						✓	✓		✓
 CSI	✓	✓				✓	✓		✓			✓
 CoLL										✓		
 CeTA		✓						✓				
 CoLL-Saigawa	✓											✓
 ConCon			✓					✓			✓	
 CO3			✓								✓	
 infChecker											✓	
 CSI ^{ho}				✓								
 AGCP					✓							
 Moca											✓	
 FORT-h					✓	✓	✓		✓	✓		
 SOL				✓								
 nonreach											✓	

2021

TRS

CPF-TRS

CTRS

GCR

NFP













UNR














UNC

COM

INF

SRS

 ACP	✓	✓	✓						✓	✓		✓
 CSI	✓	✓				✓	✓		✓			✓
 CoLL										✓		
 CeTA		✓										
 CoLL-Saigawa	✓											✓
 CO3			✓									✓
 infChecker											✓	
 FORTify	✓				✓		✓		✓	✓		
 CONFident	✓		✓									✓
 AGCP					✓							
 NaTT											✓	
 FORT-h					✓	✓	✓		✓	✓		

 ACP	✓	✓	✓						✓	✓		✓
 CSI	✓	✓				✓	✓		✓			✓
 CoLL										✓		
 CeTA		✓										
 Hakusan	✓											✓
 Toma											✓	
 CO3			✓								✓	
 infChecker											✓	
 FORTify		✓			✓	✓	✓		✓	✓		
 CONFident	✓		✓					✓				✓
 AGCP					✓							
 NaTT											✓	
 FORT-h		✓			✓	✓	✓		✓	✓		

2023

TRS

CTRS

GCR

NFP

UNR
















CSR

UNC

COM

INF

SRS

	TRS		CTRS		GCR	NFP	UNR	CSR	UNC	COM	INF	SRS
 ACP	✓		✓				✓		✓	✓		✓
 CSI	✓					✓	✓		✓			✓
 CoLL										✓		
 CeTA	✓									✓	✓	✓
 Hakusan	✓											✓
 Toma											✓	
 CO3			✓								✓	
 infChecker											✓	
 FORTify	✓				✓	✓	✓		✓	✓		
 CONFident	✓		✓					✓				✓
 AGCP					✓							
 NaTT											✓	
 FORT-h	✓				✓	✓	✓		✓	✓		
 ConfCSR								✓				
 nonreach											✓	

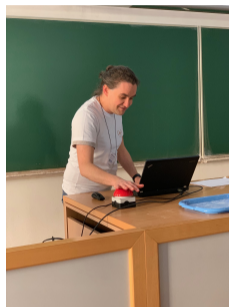
► CoCo is powered by StarExec



► CoCo is powered by StarExec



► exciting to watch

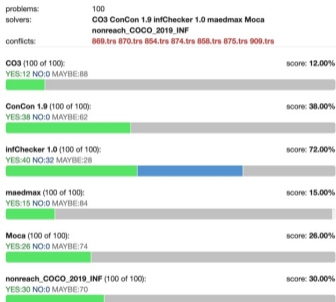


- ▶ CoCo is powered by StarExec

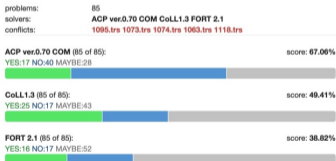


- ▶ exciting to watch, partly due to real-time **yes / no conflicts**

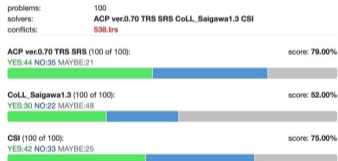
INF



COM



TRS



final slide CoCo 2023 presentation

- ▶ CoCo 2024 during IWC 2024 ?

final slide CoCo 2023 presentation

- ▶ CoCo 2024 during IWC 2024 ?
- ▶ new T-shirt ?

final slide CoCo 2023 presentation

- ▶ CoCo 2024 during IWC 2024 ?
- ▶ new T-shirt ?
- ▶ new category on confluence of logically constrained rewrite systems

LCTRS

final slide CoCo 2023 presentation

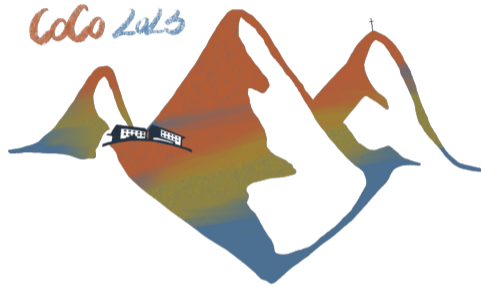
- ▶ CoCo 2024 during IWC 2024 ?
- ▶ new T-shirt ?
- ▶ new category on confluence of logically constrained rewrite systems
- ▶ new format and infrastructure

LCTRS

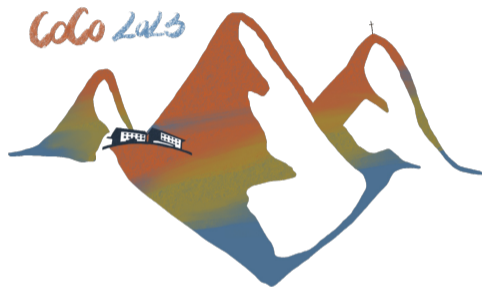


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<https://ari-cops.uibk.ac.at/liveview/2024.html>



T shirt 20 €

<https://ari-cops.uibk.ac.at/liveview/2024.html>

2023

TRS

CTRS

GCR

NFP

UNR
















CSR















UNC

COM

INF

SRS

	TRS		CTRS		GCR	NFP	UNR	CSR	UNC	COM	INF	SRS
 ACP	✓		✓				✓		✓	✓		✓
 CSI	✓					✓	✓		✓			✓
 CoLL										✓		
 CeTA	✓									✓	✓	✓
 Hakusan	✓											✓
 Toma											✓	
 CO3			✓								✓	
 infChecker											✓	
 FORTify	✓				✓	✓	✓		✓	✓		
 CONFident	✓		✓					✓				✓
 AGCP					✓							
 NaTT											✓	
 FORT-h	✓				✓	✓	✓		✓	✓		
 ConfCSR								✓				
 nonreach											✓	

	TRS	LCTRS	CTRS	GCR	NFP	UNR	CSR	UNC	COM	INF	SRS
 ACP	✓		✓			✓		✓	✓		✓
 CSI	✓				✓	✓		✓			✓
 CeTA	✓								✓	✓	✓
 Hakusan	✓										✓
 Moca										✓	
 CO3			✓							✓	
 infChecker										✓	
 FORTify	✓			✓	✓	✓		✓	✓		
 CONFident	✓		✓				✓				✓
 AGCP				✓							
 NaTT										✓	
 FORT-h	✓			✓	✓	✓		✓	✓		
 CRaris		✓									
 crest		✓									

Outline

1. Acknowledgements

2. History

3. 2024

Categories

Rules

Live View

4. Awards

5. Outlook

Categories

TRS	confluence of first-order term rewrite systems
CTRS	confluence of first-order conditional term rewrite systems
HRS	confluence of higher-order rewrite systems
GCR	ground-confluence of many-sorted first-order rewrite systems
LCTRS	confluence of logically constrained term rewrite systems
NFP	normal form property of first-order rewrite systems
UNR	unique normal forms wrt reduction of first-order rewrite systems
UNC	unique normal forms wrt conversion of first-order rewrite systems
COM	commutation of first-order rewrite systems
INF	infeasibility
SRS	confluence of string rewrite systems
CSR	confluence of context-sensitive rewriting

Categories

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Competition Rules

▶ Scoring

- ▶ 100 random problems per category, using seed digits provided by panel members
- ▶ tools output YES, NO or MAYBE on first line followed by proof
- ▶ separate rankings for YES and NO and combined YES/NO answers
- ▶ winning tools of 2023 participate as demonstration tools in 2024

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 - ▶ winning tools of 2023 participate as demonstration tools in 2024
- ▶ **Secret Problems**
 - ▶ guaranteed to be selected
 - ▶ at most two problems per category per tool

Secret Problems

0 secret problems submitted to CoCo 2023

Secret Problems

8 secret problems submitted to CoCo 2024:

- ▶ 2 by Takahito Aoto UNR 1606 1607

$$h(f(x), b) \rightarrow c$$

$$b \rightarrow a$$

$$c \rightarrow f(c)$$

$$a \rightarrow b$$

$$f(g(b), b) \rightarrow f(g(a), a)$$

$$f(g(x), a) \rightarrow f(g(a), a)$$

- ▶ 2 by René Thiemann INF 1612 1613

$$\text{ack}(0, n) \rightarrow s(n)$$

$$\text{isNat}(0) \rightarrow \text{true}$$

$$\text{isNat}(\text{true}) \rightarrow \text{false}$$

$$\text{ack}(s(m), 0) \rightarrow \text{ack}(m, s(0))$$

$$\text{isNat}(s(m)) \rightarrow \text{isNat}(m)$$

$$\text{isNat}(\text{false}) \rightarrow \text{false}$$

$$\text{ack}(s(m), s(n)) \rightarrow \text{ack}(m, \text{ack}(s(m), n))$$

$$\text{seven} \rightarrow s(s(s(s(s(s(O)))))))$$

$$\text{isNat}(\text{ack}(\text{seven}, \text{seven})) \stackrel{?}{\approx} \text{true}$$

- ▶ 2 by Naoki Nishida LCTRS 1610 1611

- ▶ 2 by Jonas Schöpf LCTRS 1608 1609

Competition Rules

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- ▶ Secret Problems
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Problem Selection

Example: ARI-COPS queries for UNR category

① 1606 or 1607

② limit:98,361 1..1605 trs !CR:YES

Problem Selection

Example: ARI-COPS queries for UNR category

① 1606 or 1607

returns 2 secret problems

② limit:98,361 1..1605 trs !CR:YES

▶ secret problems have numbers 1606 ... 1613

Problem Selection

Example: ARI-COPS queries for UNR category

① 1606 or 1607

returns 2 secret problems

② `limit:98,361 1..1605 trs !CR:YES`

- ▶ secret problems have numbers 1606 ... 1613
- ▶ seed digits of panel members

Problem Selection

Example: ARI-COPS queries for UNR category

① 1606 or 1607

returns 2 secret problems

② `limit:98,361 1..1605 trs !CR:YES`

- ▶ secret problems have numbers 1606 ... 1613
- ▶ seed digits of panel members
- ▶ 1605 problems in ARI-COPS database

Problem Selection

Example: ARI-COPS queries for UNR category

① 1606 or 1607

returns 2 secret problems

② `limit:98,361 1..1605 trs !CR:YES`

- ▶ secret problems have numbers 1606 ... 1613
- ▶ seed digits of panel members
- ▶ 1605 problems in ARI-COPS database
- ▶ exclude TRSs that are guaranteed to be confluent

Problem Selection

Example: ARI-COPS queries for UNR category

- 1 1606 or 1607
returns 2 secret problems
 - 2 `limit:98,361 1..1605 trs !CR:YES`
returns 98 problems which are non-confluent
- ▶ secret problems have numbers 1606 ... 1613
 - ▶ seed digits of panel members
 - ▶ 1605 problems in ARI-COPS database
 - ▶ exclude TRSs that are guaranteed to be confluent

Competition Rules

▶ Scoring

- ▶ 100 random problems per category, using seed digits provided by panel members
- ▶ tools output YES, NO or MAYBE on first line followed by proof
- ▶ separate rankings for YES and NO and combined YES/NO answers
- ▶ winning tools of 2023 participate as demonstration tools in 2024

▶ Secret Problems

- ▶ guaranteed to be selected
- ▶ at most two problems per category per tool

▶ Incorrect Results

- ▶ tools with incorrect results (observed during live competition due to YES/NO conflict, or communicated afterwards by tool authors to SC) are excluded from results table

Competition Rules

- ▶ Scoring
 - ▶ 100 random problems per category, using seed digits provided by panel members
 - ▶ tools output YES, NO or MAYBE on first line followed by proof
 - ▶ separate rankings for YES and NO and combined YES/NO answers
 - ▶ winning tools of 2023 participate as demonstration tools in 2024
- ▶ Secret Problems
 - ▶ guaranteed to be selected
 - ▶ at most two problems per category per tool
- ▶ **Incorrect Results**
 - ▶ tools with incorrect results (observed during live competition due to YES/NO conflict, or communicated afterwards by tool authors to SC) are excluded from results table
 - ▶ (corrected) tools are available from **CoCoWeb** for testing



Tools

2023

CSRS

CTRS

SRS

TRS

2022

2021

2020

2019

2018

2017

2016

2015

2014

2013

2012

Enter a **rewrite system**, upload a file or import a Cop:

```
1  {CONDITIONTYPE ORIENTED)
2  {VAR x)
3  {RULES
4    a -> b
5    a -> c
6    b -> c | b == c
7  }
8  {COMMENT
9    doi: 10.1007/3-540-54317-1_99
10   [58] Example 1.1
11   submitted by: Thomas Sternagel and Aart Middeldorp
12  }
13
```

property:
 timeout:
submit this problem to



Tools

2023

CSRS

CTRS

ACP

CO3

CONFident

SRS

TRS

2022

2021

2020

2019

2018

2017

2016

2015

2014

Enter a **rewrite system**, upload a file or import a Cop:

```

1 (CONDITIONTYPE ORIENTED)
2 (VAR x)
3 (RULES
4   a -> b
5   a -> c
6   b -> c | b == c
7 )
8 (COMMENT
9   doi: 10.1007/3-540-54317-1_99
10  [58] Example 1.1
11  submitted by: Thomas Sternagel and Aart Middeldorp
12 )
13
```

 property:

 timeout:

Results

Took 0.01s

NO

```

Succeeded in reading "/home/www/colo6-
c703/cocoweb/session/k4hg4kete2bc30c8ssccd8t3a0/tmp.trs".
(CONDITIONTYPE ORIENTED)
(RIII FS
```

 search1605 problems matched ([download](#)) view: [problems](#) | [results](#) order: [asc](#) | [desc](#) download: [all data](#)« back  next »[1.ari](#)

```
; @author Takahito Aoto
; @author Junichi Yoshida
; @author Yoshihito Toyama
; @doi 10.1007/BFb0027006
; @cops 1
; [1] Example 6
(format TRS)
(fun F 2)
(fun f 2)
(fun g 1)
(fun q 1)
(fun h 1)
(rule (f x y) x)
(rule (f x y) (f x (g y)))
(rule (g x) (h x))
(rule (F (g x) x) (F x (g x)))
(rule (F (h x) x) (F x (h x)))
```

YES: [well-formed](#) [trs](#) [CR](#)NO: [ctr](#) [cctr](#) [ccctr](#) [mstr](#) [lctr](#) [2trs](#) [infeasibility](#) [ground](#) [left-linear](#) [right-ground](#) [srs](#)[2.ari](#)

```
; @author Takahito Aoto
; @author Junichi Yoshida
; @author Yoshihito Toyama
; @doi 10.3217/jucs-003-11-1134
; @cops 2
; [2] Example 1
(format TRS)
(fun F 2)
```

confluence problems database (**ARI-COPS**) consists of 1605 problems

CoCo 2024 Live View

<https://ari-cops.uibk.ac.at/liveview/2024.html>

2023 Results



2023 Results



- ▶ previous winners: ACP 2012 2013 2014 2015 2019
CSI 2015 2016 2017 2018 2020 2021 2022

2023 Results



- ▶ previous winners: ACP 2012 2013 2014 2015 2019
CSI 2015 2016 2017 2018 2020 2021 2022
- ▶ 2024 participants: ACP ACP+CeTA CONFident CSI CSI+CeTA FORT-h
FORT-h+FORTify Hakusan Hakusan+CeTA

2023 Results



- ▶ previous winners: ACP 2012 2013 2014 2015 2019
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FORT-h+FORTify Hakusan Hakusan+CeTA



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CONFident at CoCo 2024

Miguel Vítores¹ Raúl Gutiérrez¹ Salvador Lucas¹

TALLINN, JULY 9TH, 2024

¹Valencian Research Institute for Artificial Intelligence
Universitat Politècnica de València
Spain

UPV

- CONFident is a tool for checking **(non-)confluence** of Generalized Term Rewriting Systems (GTRSs).
- A GTRS is a tuple $\mathcal{R} = (\Omega, \mu, H, R)$, where:
 - $\Omega = (\mathcal{F}, \Pi)$ is a signature with predicates.
 - $\mu \in M_{\mathcal{F}}$.
 - H is a set of auxiliary clauses (H is used to model the semantics of conditions).
 - R is a set of rewrite rules $\ell \rightarrow r \Leftarrow c$.
- This year, our participation involves utilizing the same tool employed in the previous year.
- In the bibliography, you can find new publications on some techniques that were unpublished last year.

An Example

- Consider the GTRS \mathcal{R} :

$$\begin{array}{ll} x \geq 0 & \text{odd}(x) \Leftrightarrow x \rightarrow^* s(0) \\ s(x) \geq s(y) \Leftrightarrow x \geq y & \text{zero}(x) \Leftrightarrow x \rightarrow^* 0 \\ \text{peven}(x) \Leftrightarrow x \rightarrow^* s(s(0)) & s(s(x)) \rightarrow x \Leftrightarrow x \geq s(0) \end{array}$$

- CONFident can prove the confluence of \mathcal{R} ... details in Salvador Lucas's talk!

- It is written in Haskell and implements the **Confluence Framework**. The tool is available here:

`http://zenon.dsic.upv.es/confident/`

- Bibliography:

- GL24** R. Gutiérrez and S. Lucas. Proving Confluence in the Confluence Framework with CONFident. *Fundamenta Informaticae* 193, to appear, 2024.
- GLV23** R. Gutiérrez, S. Lucas and M. Vítores. Proving Confluence in the Confluence Framework with CONFident. CoRR abs/2306.16330, 2023.
- Luc24** S. Lucas. Orthogonality of Generalized Term Rewriting Systems. Proc. of IWC'2024, to appear, 2024.
- LVG22** S. Lucas, M. Vítores and R. Gutiérrez. Proving and disproving confluence of context-sensitive rewriting. *J. Log. Algebraic Methods Program.* 126: 100749, 2022.

2023 Results



2023 Results



▶ previous winner: CSI 2019 2020 2021 2022

2023 Results



- ▶ previous winner: CSI 2019 2020 2021 2022
- ▶ 2024 participants: ACP ACP+CeTA CONFident CSI CSI+CeTA Hakusan Hakusan+CeTA

2023 Results



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Hakusan+CeTA
- ▶ **noko-leipzig** produced most NO answers in 2019

2023 Results



- ▶ previous winner: CSI 2019 2020 2021 2022
- ▶ 2024 participants: ACP ACP+CeTA CONFident CSI CSI+CeTA **Hakusan**
Hakusan+CeTA
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Hakusan v0.11 (Kawano, Hirokawa, Shintani, JAIST)

confluence tool for left-linear TRSs



Hakusan v0.11 (Kawano, Hirokawa, Shintani, JAIST)

confluence tool for **left-linear** TRSs

1 CeTA-certifiable proofs

joint work with Kim & Thiemann (CPP 2024)



Hakusan v0.11 (Kawano, Hirokawa, Shintani, JAIST)

confluence tool for **left-linear** TRSs

- 1 CeTA-certifiable proofs joint work with Kim & Thiemann (CPP 2024)
- 2 **rule removal** by rule labeling & critical pair systems (LMCS & IWC 2024)

confluence tool for **left-linear** TRSs

- ① CeTA-certifiable proofs joint work with Kim & Thiemann (CPP 2024)
- ② **rule removal** by rule labeling & critical pair systems (LMCS & IWC 2024)

Theorem (critical pair system)

$CR(\mathcal{R}) \Leftrightarrow CR(\mathcal{S})$ if \mathcal{R} is LL, $\mathcal{S} \subseteq \mathcal{R}$, $PCP(\mathcal{R}) \subseteq \downarrow_{\mathcal{R}}$, $SN(\mathcal{P}/\mathcal{R})$, and $\mathcal{R}|_{\mathcal{S}} \subseteq \rightarrow_{\mathcal{S}}^*$

- $\mathcal{P} = \left\{ \begin{array}{l} s \rightarrow t \\ s \rightarrow u \end{array} \middle| t \xleftrightarrow[\mathcal{R}]{\Leftarrow} s \xrightarrow[\mathcal{R}]{\epsilon} u \text{ is parallel critical peak but not } t \xleftrightarrow[\mathcal{S}]{\Leftarrow^*} u \right\}$
- $\mathcal{R}|_{\mathcal{S}} = \{ \ell \rightarrow r \in \mathcal{R} \mid \mathcal{F}un(\ell) \subseteq \mathcal{F}un(\mathcal{S}) \}$

Confluence Proof by Rule Removal

consider left-linear TRS \mathcal{R} :

$$s(p(x)) \xrightarrow{1} p(s(x))$$

$$p(s(x)) \xrightarrow{2} x$$

$$\infty \xrightarrow{3} s(\infty)$$

Confluence Proof by Rule Removal

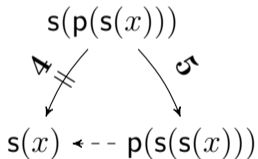
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① $CR(\mathcal{R}) \iff CR(\{3\})$ by critical pair system:

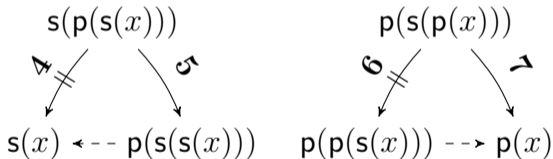


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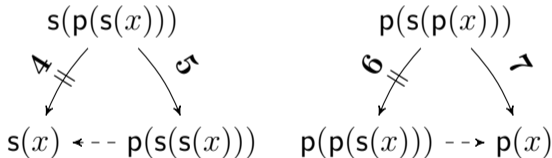
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$SN(\{4, 5, 6, 7\}/\mathcal{R})$

Confluence Proof by Rule Removal

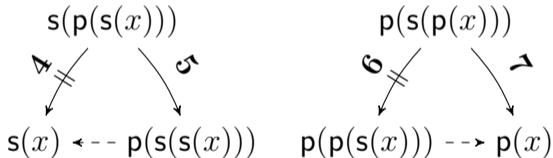
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$$\mathcal{R}|_{\{3\}} = \{3\} \subseteq \rightarrow_{\{3\}}^*$$

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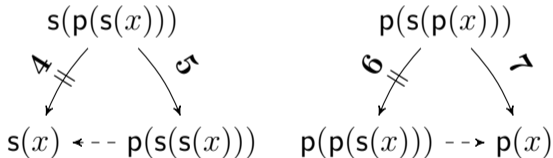
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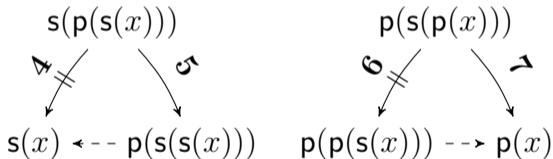
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② $CR(\{\mathbf{3}\}) \iff CR(\emptyset)$ by rule labeling

Confluence Proof by Rule Removal

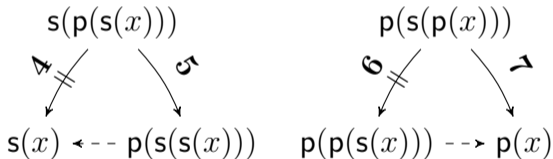
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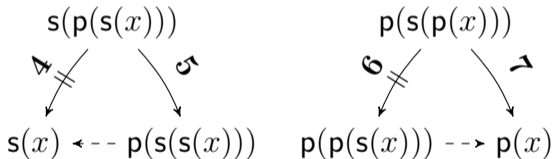
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$$\mathcal{R}|_{\{3\}} = \{3\} \subseteq \rightarrow_{\{3\}}^*$$

2 $CR(\{3\}) \iff CR(\emptyset)$ by rule labeling

3 $CR(\emptyset)$ is trivial

2023 Results



2023 Results



▶ previous winner: infChecker 2019 2020 2021 2022

2023 Results



- ▶ previous winner: infChecker 2019 2020 2021 2022
- ▶ 2024 participants: CO3 infChecker **Moca** **Moca+CeTA** NaTT

2023 Results



- ▶ previous winner: infChecker 2019 2020 2021 2022
- ▶ 2024 participants: CO3 **infChecker** **Moca** Moca+CeTA **NaTT**



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infChecker at CoCo 2024

Raúl Gutiérrez¹ Salvador Lucas¹

TALLINN, JULY 9TH, 2024

¹Valencian Research Institute for Artificial Intelligence
Universitat Politècnica de València
Spain

UPV

- infChecker is a tool for checking **(in)feasibility of goals**
 $\mathcal{G} = \{F_i\}_{i=1}^m$, where $F_i = (s_{ij} \bowtie_{ij} t_{ij})_{i=1}^{n_i}$.
- \bowtie_{ij} represents **predicates** on terms defined by provability of goals $s \bowtie_{ij} t$ with respect to a *first-order theories* $\text{Th}_{\bowtie_{ij}}$.
- \bowtie_{ij} can be one of the following predicates:
 - One (CS-)rewriting step (\rightarrow , \rightarrow).
 - Zero or more (CS-)rewriting steps (\rightarrow^* , \rightarrow^*).
 - One or more (CS-)rewriting steps (\rightarrow^+ , \rightarrow^+).
 - Subterm ($\mid \geq$) and strict subterm ($\mid >$).
 - (CS-)Joinability ($\rightarrow^* \leftarrow$, $\rightarrow^* \leftarrow /$).
 - One (CS-)convertibility step ($\leftarrow \rightarrow$, \leftarrow / \rightarrow).
 - Zero or more (CS-)convertibility steps ($\leftarrow \rightarrow^*$, $\leftarrow / \rightarrow^*$).
- This year, our participation involves utilizing the same tool employed in the previous year.

An Example

- Given the TRS $\mathcal{R} = \{a \rightarrow c(b), b \rightarrow c(b)\}$, infChecker can prove the nonloopingness of a as the infeasibility of

$$(\{\overline{\mathcal{R}}, Th_{\succeq}\}, \{\neg(x, y)(a \rightarrow x, x \rightarrow^* y, y \succeq a)\})$$

by obtaining the following structure over $\mathbb{N} \cup \{-1\}$:

$$\begin{array}{ll} a^{\mathcal{A}} = -1 & b^{\mathcal{A}} = 1 \\ c^{\mathcal{A}}(x) = x & x \rightarrow^{\mathcal{A}} y \Leftrightarrow x \leq 1 \wedge y \geq 1 \\ x (\rightarrow^*)^{\mathcal{A}} y \Leftrightarrow x \leq y & x \succeq^{\mathcal{A}} y \Leftrightarrow x \leq y \end{array}$$

- It is written in Haskell and implements the **Feasibility Framework**. The tool is available here:

`http://zenon.dsic.upv.es/infChecker/`

- Bibliography:

GL20 R. Gutiérrez and S. Lucas. Automatically Proving and Disproving Feasibility Conditions. In Proc. of IJCAR'2020, LNCS 12167:416–435. Springer, 2020.

Luc19 S. Lucas. Proving semantic properties as first-order satisfiability. Artificial Intelligence 277, paper 103174, 24 pages, 2019.

LG18 S. Lucas and R. Gutiérrez. Use of Logical Models for Proving Infeasibility in Term Rewriting. Information Processing Letters, 136:90-95, 2018.

Moca 0.3

Yusuke Oi

Nao Hirokawa

Teppei Saito

JAIST

CoCo 2024

Maximal ordered completion with approximation

Would you like some coffee? Here it is!

Moca solves infeasibility problem $s \rightarrow^* t$ of CTRS \mathcal{R} as follows:

Maximal ordered completion with approximation

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Moca solves infeasibility problem $s \rightarrow^* t$ of CTRS \mathcal{R} as follows:

- 1 reformulate problem as $T \rightarrow^* F$ of $\mathcal{R} \cup \{T \rightarrow F \Leftarrow s \rightarrow^* t\}$

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- 2 unravel/split-if CTRS into TRS \mathcal{R}'

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- 3 approximate infeasibility as word problem $T \approx_{\mathcal{R}'} F$

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- 4 approximate further (e.g., adding $f(x, y) \approx x$)

Maximal ordered completion with approximation

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Maximal ordered completion with approximation

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- 5 solve word problem by (maximal) ordered completion

news: Moca meets CeTA!

NaTT in CoCo 2024

Akihisa Yamada @ AIST

NaTT in CoCo

- NaTT a **termination prover** for **plain** term rewriting
- In CoCo 2021:
 - participated **INF** category with an easy checker [Sternagel & Yamada '19]
 - weak but fast
- In CoCo 2022:
 - **coWPO** for INF [IJCAR '22]
 - not too weak, but slow
- In CoCo 2024:
 - no time for research...
 - only adapted parser for ARI

2023 Results



2023 Results



- ▶ previous winners: CO3 2014 ConCon 2015 2016 2017 2018 2020 ACP 2019
CONFident 2021 2022

2023 Results



- ▶ previous winners: CO3 2014 ConCon 2015 2016 2017 2018 2020 CONFident 2021 2022 ACP 2019
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2023 Results



- ▶ previous winners: CO3 2014 ConCon 2015 2016 2017 2018 2020 CONFident 2021 2022 ACP 2019
- ▶ 2024 participants: ACP CO3 CONFident

CO3 (Ver. 2.5)

a COnverter for proving COnfluence of COnditional TRSs

Naoki Nishida Misaki Kojima
Nagoya University, Japan

Overview

CO3 proves confluence of 3-DCTRSs or infeasibility of conditions by using

- very simple termination/confluence criteria for TRSs,
- the improved sequential **unraveling** \mathcal{U}_{conf} [Gmeiner et al, 13],
- **narrowing trees** [Nishida & Maeda, 18], and
- reduction of confluence of join or semi-equational CTRSs to that of oriented ones

Infeasibility and Confluence Criterion

- Condition c is infeasible w.r.t. DCTRS \mathcal{R} if $\mathcal{U}_{conf}(\mathcal{R})$ is right-linear and a **narrowing tree for c** defines \emptyset [Maeda et al, 19]
- Syntactically deterministic 3-CTRSs \mathcal{R} is confluent if either
 - ▶ \mathcal{R} is weakly left-linear and $\mathcal{U}_{conf}(\mathcal{R})$ is confluent [Gmeiner et al, 13]
 - or
 - ▶ $\mathcal{U}_{conf}(\mathcal{R})$ is terminating and right-linear
and $\forall \langle s, t \rangle \leftarrow c \in CP(\mathcal{R}), (c = \epsilon \wedge s = t) \vee$ “ c is infeasible” [Maeda et al, 19]

- Added a **new disproof criterion** for confluence of \mathcal{R}

[Ver. 2.5]

2023 Results



2023 Results



▶ previous winner: AGCP 2015 2016 2017 2018 2019 2020 2021 2022

2023 Results



- ▶ previous winner: AGCP 2015 2016 2017 2018 2019 2020 2021 2022
- ▶ 2024 participants: AGCP FORT-h FORT-h+ FORTify

2023 Results



- ▶ previous winner: AGCP 2015 2016 2017 2018 2019 2020 2021 2022
- ▶ 2024 participants: **AGCP** FORT-h FORT-h + FORTify

AGCP (Automated Ground Confluence Prover)

Takahito Aoto

A ground confluence prover for many-sorted TRSs

- An entrant of **GCR** category
- Written in Standard ML of New Jersey (SML/NJ)
- Methods:
 - rewriting induction for bounded convertibility
 - equivalent transformations, disproving methods
- Based on:

*Improvements of the Rewriting Induction Approach
for proving GCR, Aoto/Toyama/Kimura, FSCD 2017*

We couldn't make any efforts on AGCP this year.

2023 Results



▶ CoLL had most YES answers

2023 Results



- ▶ CoLL had most YES answers
- ▶ previous winners: FORT 2019 ACP 2020 CoLL 2021 2022

2023 Results



- ▶ CoLL had most YES answers
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- ▶ 2024 participants: ACP ACP+CeTA FORT-h FORT-h+FORTify

2023 Results



- ▶ CoLL had most YES answers
- ▶ previous winners: FORT 2019 ACP 2020 CoLL 2021 2022
- ▶ 2024 participants: ACP ACP+CeTA **FORT-h** FORT-h+FORTify



FORT-h 2.1

Fabian Mitterwallner

Aart Middeldorp

University of Innsbruck

FORT-h



property



linear variable-separated



TRS

$$\forall s \exists t (s \rightarrow^* t \wedge \neg \exists u (t \rightarrow u)) \\ \Rightarrow \exists v (s \twoheadrightarrow v \vee v \xrightarrow{\epsilon} t)$$



yes | no | ?

property is arbitrary formula in first-order theory of rewriting

- ▶ convenient web interface
- ▶ `https://fortissimo.uibk.ac.at/fort\(ify\)/`

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CoCo 2024 Categories

COM GCR NFP TRS UNC UNR

- ▶ convenient web interface
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CoCo 2024 Categories

COM

GCR

NFP

TRS

UNC

UNR

most YES results in 2023

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CoCo 2024 Categories

COM GCR NFP TRS UNC **UNR**

most YES results in 2023

Literature

Aart Middeldorp, Alexander Lochmann and Fabian Mitterwallner

First-Order Theory of Rewriting for Linear Variable-Separated Rewrite Systems: Automation, Formalization, Certification

Journal of Automated Reasoning 67(2), 2023

doi: [10.1007/s10817-023-09661-7](https://doi.org/10.1007/s10817-023-09661-7)

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- ▶ FORT-h won **RELIABILITY** category in 2023
- ▶ FORT-h 2.1 accepts ARI format

CoCo 2024 Categories

COM GCR NFP TRS UNC **UNR**

most YES results in 2023

Literature

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2023 Results

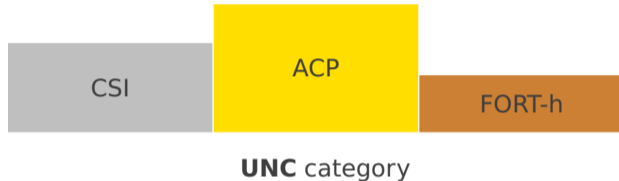


2023 Results



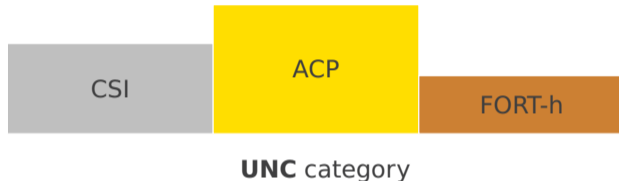
▶ previous winners: CSI 2017 ACP 2018 2019 2020 2021 2022

2023 Results



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2023 Results



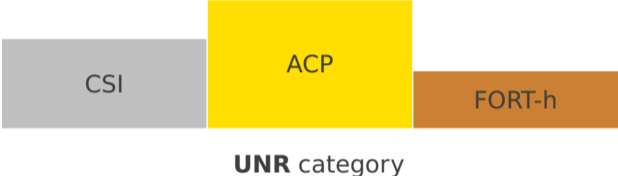
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ACP (Automated Confluence Prover)

Takahito Aoto

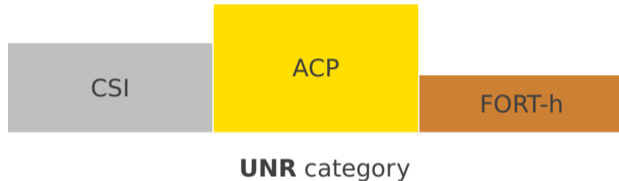
- ACP entered to **COM/CTRS/SRS/TRS/UNR/UNC**
- ACP+CeTA entered to **COM/SRS/TRS**
- Written in Standard ML of New Jersey (SML/NJ)
- Version: 0.10 (2009) ... 0.74 (2024)
- Implementing **multiple direct methods** and **divide-and-conquer methods**
- New features:
 - (i) **UNR**: (theoretically extended and) revised
Proving Uniqueness of Normal Forms w.r.t. Reduction of Term Rewriting Systems, T. Aoto, LOPSTR 2024, to appear.
 - (ii) **COM**: Certificates generation is extended and revised.

2023 Results



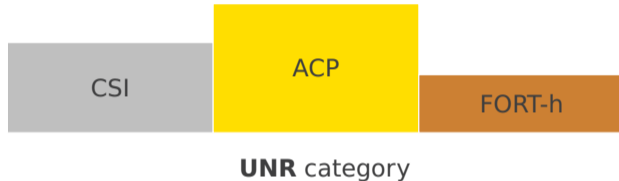
- ▶ FORT-h had most YES answers

2023 Results



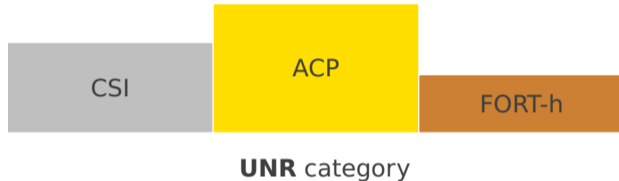
- ▶ FORT-h had most YES answers
- ▶ previous winner: CSI 2017 2018 2019 2020 2021 2022

2023 Results



- ▶ FORT-h had most YES answers
- ▶ previous winner: CSI 2017 2018 2019 2020 2021 2022
- ▶ 2024 participants: ACP CSI FORT-h FORT-h + FORTify

2023 Results



- ▶ FORT-h had most YES answers
- ▶ previous winner: CSI 2017 2018 2019 2020 2021 2022
- ▶ 2024 participants: ACP CSI FORT-h FORT-h+ **FORTify**

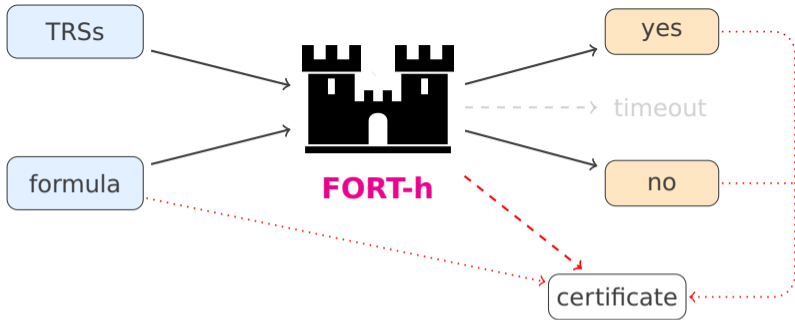


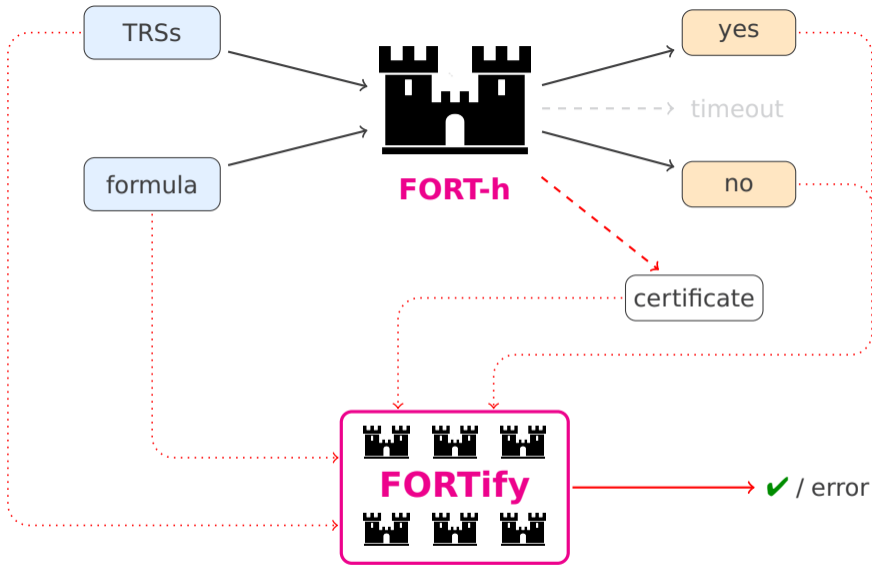
FORTify 2.1

Fabian Mitterwallner

Aart Middeldorp

University of Innsbruck





- ▶ code generated from formalization of decision procedure in Isabelle/HOL
- ▶ [https://fortissimo.uibk.ac.at/fort\(ify\)/](https://fortissimo.uibk.ac.at/fort(ify)/)

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CoCo 2024 Categories

COM GCR NFP TRS UNC UNR (with FORT-h)

- ▶ code generated from formalization of decision procedure in Isabelle/HOL
- ▶ [https://fortissimo.uibk.ac.at/fort\(ify\)/](https://fortissimo.uibk.ac.at/fort(ify)/)

CoCo 2024 Categories

COM GCR NFP TRS UNC UNR (with FORT-h)

Literature

Aart Middeldorp, Alexander Lochmann and Fabian Mitterwallner

First-Order Theory of Rewriting for Linear Variable-Separated Rewrite Systems: Automation, Formalization, Certification

Journal of Automated Reasoning 67(2), 2023

doi: [10.1007/s10817-023-09661-7](https://doi.org/10.1007/s10817-023-09661-7)

2023 Results



2023 Results



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CSI 1.2.7

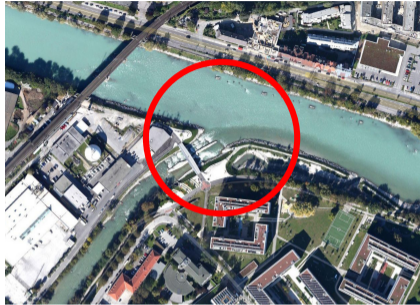
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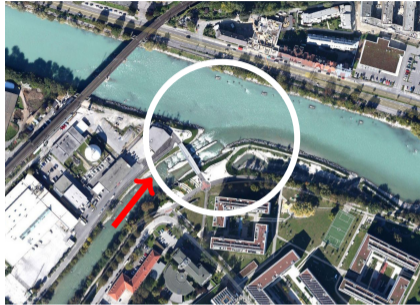


[Google Maps]



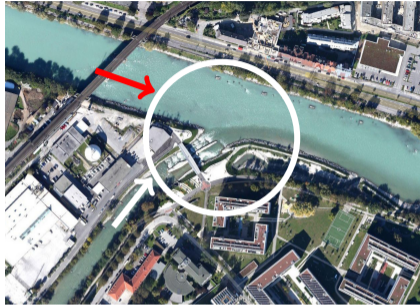
[Google Maps]

C



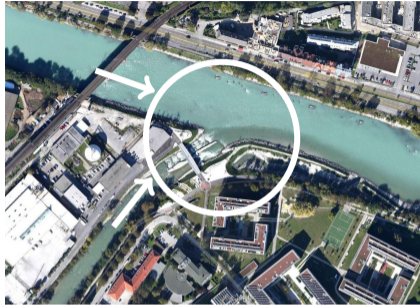
[Google Maps]

CS



[Google Maps]

CSI



[Google Maps]

CSI 1.2.7

- ▶ open source
- ▶ convenient web interface
- ▶ `http://cl-informatik.uibk.ac.at/software/csi/`

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CoCo 2024 Categories

- ▶ SRS TRS UNC UNR NFP
- ▶ SRS TRS with CeTA

- ▶ open source
- ▶ convenient web interface
- ▶ <http://cl-informatik.uibk.ac.at/software/csi/>

CoCo 2024 Categories

- ▶ **SRS** **TRS** UNC UNR **NFP** **1st place in 2023**
- ▶ SRS TRS with CeTA

- ▶ open source
- ▶ convenient web interface
- ▶ <http://cl-informatik.uibk.ac.at/software/csi/>

CoCo 2024 Categories

- ▶ SRS TRS UNC UNR NFP
- ▶ SRS TRS with CeTA

No New Features in 2024

- ▶ CSI uses ARI → COPS conversion tool

2023 Results



2023 Results



▶ previous winner: CONFident 2022

2023 Results



- ▶ previous winner: CONFident 2022
- ▶ 2024 participants: CONFident

2023 Results



2023 Results



- ▶ 2024 participants: CeTA FORTify

2023 Results



▶ 2024 participants: **CeTA** FORTify



CoCo 2024 Participant: CeTA 3.2

Dohan Kim,¹ Christina Kirk,¹ Teppei Saito² and René Thiemann¹

1: University of Innsbruck, Austria

2: Japan Advanced Institute of Science and Technology, Japan

CeTA 3.2



- CeTA: certifier of various properties, verified in Isabelle/HOL
- mostly developed by Computational Logic Group in Innsbruck
- several confluence techniques supported, see a complete list at:
<http://cl-informatik.uibk.ac.at/software/ceta/>
- usage in CoCo: certify proofs and disproofs of
 - confluence
 - commutation
 - infeasibility (new in 2024: feasibility)
- usage in ARI-database: certify YES/NO for CR/COM/INF-tags

New techniques in CeTA 3.2 in comparison to 2023

- several **new term orders** for non-CR/COM and infeasibility proofs
 - CoWPO and WPO (weighted path order)
 - generalized WPO and MSPO (monotonic semantic path order)
 - polynomial interpretations over $\mathbb{Z}_{\leq 0}$
- non-joinability proofs via **finite sets of reachable terms**
- **feasibility** proofs via explicit conditional rewrite sequences (no certificate generating tool yet)
- **infeasibility proofs** by unraveling and Knuth–Bendix completion (used by Moca)

New CPF 3 format in 2024

- converter from CPF 2 available (based on xsltproc)
- more consistent confluence proofs, e.g., same format for joining sequences
- better support for competitions, e.g., overwrite input and answer in CPF3
- more concise certificates
 - rule- and term-indexing
 - removed superfluous XML-elements

```
<polynomial><sum>  
  <polynomial><variable>1</variable></polynomial>  
  <polynomial><coefficient><integer>2</integer></coefficient></polynomial>  
</sum></polynomial>
```

to specify $x_1 + 2$ in CPF 2 becomes the following in CPF 3:

```
<sum><variable>1</variable><integer>2</integer></sum>
```

2023 Results



2023 Results



- ▶ 2024 participants: ACP CSI FORT-h Hakusan **Moca**

2023 Results



LCTRS category



2023 Results



▶ new category supported by FWF-JSPS ARI project



2023 Results



- ▶ new category supported by FWF–JSPS ARI project
- ▶ 2024 participants: **CRaris crest**



CRaris

a CR checker for LCTRSs in ARI style

Naoki Nishida Misaki Kojima

Nagoya University, Japan

Overview

CRaris, which is a part of Crisys2, proves confluence of LCTRSs written in ARI style

- Crisys2 is a rewriting-induction tool for LCTRSs

Supported SMT-LIB Theories

Core, Ints, FixedSizeBitVecotrs

Implemented Confluence Criteria

- weak orthogonality (left-linearity + triviality of CPs) [Kop and Nishida, 2013]
- termination + triviality of CPs [Schöpf and Middeldorp, 2023]

Implemented Termination Criteria

DP framework for LCTRSs [Kop, 2013] with

- SCC processor
- singleton self-looping removal processor for BV-LCTRSs [Matsumi et al, 2023]



crest 0.8

Jonas Schöpf Aart Middeldorp

University of Innsbruck



► Constrained REwriting Software Tool

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- ▶ confluence and termination analysis of logically constrained rewrite systems

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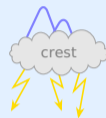
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CoCo 2024 Categories

LCTRS

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CoCo 2024 Categories

LCTRS

and the 2024 winners are ...



<https://ari-cops.uibk.ac.at/liveview/2024.html>

Outline

1. Acknowledgements
2. History
3. 2024
- 4. Awards**
5. Outlook

The logo consists of three brown, textured circles arranged horizontally, resembling cocoa beans.

the steering committee of the

12th Confluence Competition

awarded

TOOL by *TOOL* authors

the

First Place in the ? category

Obergurgl, 23 August 2023

Awards

- ▶ top three tools in each category (excluding tool + certifier)

Awards

- ▶ top three tools in each category (excluding tool + certifier)
- ▶ certifiers based on total number of certified answers

CERTIFICATION

Awards

- ▶ top three tools in each category (excluding tool + certifier)
- ▶ certifiers based on total number of certified answers
- ▶ top three tools that produce most certifiable answers

CERTIFICATION

RELIABILITY

Awards

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- ▶ certifiers based on total number of certified answers
- ▶ top three tools that produce most certifiable answers

CERTIFICATION

RELIABILITY

no **Award Ceremony**: certificates will be sent by email

Outline

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Outlook

- ▶ CoCo 2025 during IWC 2025 ?






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- ▶ new T-shirt ?

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14th International School on Rewriting (ISR 2024)
August 25 — September 1
Obergurgl



<http://cl-informatik.uibk.ac.at/isr24/>